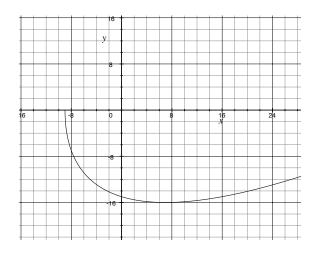
## **East Los Angeles College Department of Mathematics**

## Math 262 Test 4-Take Home

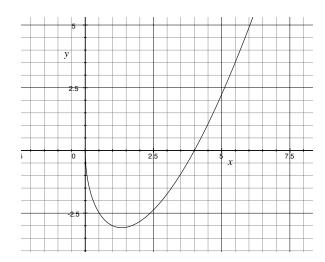
## Show your work for credit.

Let 
$$\begin{array}{c} x = t^2 - 9 \\ y = t^2 - 8t \end{array}$$
 be parametric equations.

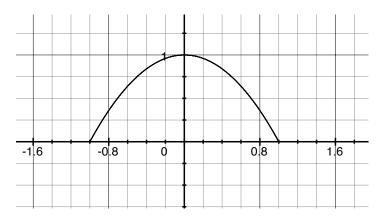


- 1. Draw an arrow indicating the direction of motion.
- 2. Find  $\frac{dy}{dx}$  when t=4
- 3. Find the equation of the tangent line when t=4.
- 4. Find the points where the slope of the tangent line equals  $\frac{1}{2}$
- 5. Find the points where the tangent line is horizontal.

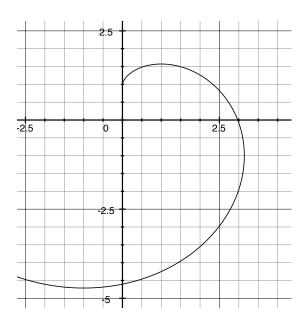
6. Let 
$$x=t^2$$
  $y=t^3-4t$  be parametric equations. Determine the interval for t in which the curve is concave up.



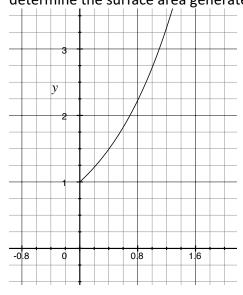
7. Let  $\begin{array}{c} x=\sin{(t)} \\ y=\cos^2(t) \end{array}$  for  $0\leq t\leq \frac{\pi}{2}$ . Compute the area under the parametric curve



8. Let x = sin(t) - tcos(t) for  $0 \le t \le 2$  be parametric equations. Determine the arc length for the curve.



9. Let x=t  $y=e^t$  for  $0 \le t \le 1$  be parametric equations. If you rotate the curve about the x-axis, determine the surface area generated.



Determine the limits of the following sequences.

10. 
$$\left\{\frac{3n^3}{n^3+1}\right\}$$

11. 
$$\{e^{-n}n^{10}\}$$

$$12. \left\{ \left(\frac{5+n}{n}\right)^n \right\}$$

$$13. \left\{ \frac{n^4}{n^4+1} \right\}$$

14. 
$$\left\{\frac{(-1)^n n^4}{n^4 + 1}\right\}$$

15. 
$$\left\{ \frac{\cos(n)}{n^2+1} \right\}$$

Determine whether the series converges or diverges.

16. 
$$\sum_{k=0}^{\infty} \left(\frac{e}{\pi}\right)^k$$

$$17. \sum_{k=0}^{\infty} \left(-\frac{3}{4}\right)^k$$

18. 
$$\sum_{k=1}^{\infty} \frac{2^{k-1}}{3^{k+1}}$$

Determine whether the following telescoping series converge or diverge. Show your work by computing the sequence of partial sums.

19. 
$$\sum_{k=1}^{\infty} \left( \frac{1}{k+1} - \frac{1}{k+2} \right)$$

$$20. \ \sum_{k=1}^{\infty} \left( \sqrt{k+1} - \sqrt{k} \right)$$

What is your:

21. Test 1 Scores?

22. Test 2 Scores?

23. Test 3 Scores?

24. Name?