

Graphing Tangent and Cotangent

$$y = a \tan[kx]$$
$$k > 0$$

$$\text{Period } p = \frac{\pi}{k}$$

$$\text{Interval of One Cycle} = \left(-\frac{\pi}{2k}, \frac{\pi}{2k}\right)$$

$$\text{Vertical Asymptotes } x = -\frac{\pi}{2k} \text{ and } x = \frac{\pi}{2k}$$

$$y = a \cot[kx]$$
$$k > 0$$

$$\text{Period } p = \frac{\pi}{k}$$

$$\text{Interval of One Cycle} = \left(0, \frac{\pi}{k}\right)$$

$$\text{Vertical Asymptotes } x = 0 \text{ and } x = \frac{\pi}{k}$$

Determine the period, interval of one cycle, x-intercept, vertical asymptotes.

1. $y = \tan(2x)$

2. $y = \tan(4x)$

3. $y = \frac{1}{4} \tan\left(\frac{x}{3}\right)$

4. $y = \tan\left(\frac{x}{4}\right)$

5. $y = \frac{2}{3} \cot\left(\frac{1}{2}x\right)$

6. $y = \cot\left(\frac{1}{3}x\right)$

7. $y = -\cot(2x)$

$$8. y = -\cot(3x)$$

$$9. y = -4\tan(\pi x)$$

$$10. y = 3\tan(2\pi x)$$

$$11. y = 2\cot(3\pi x)$$

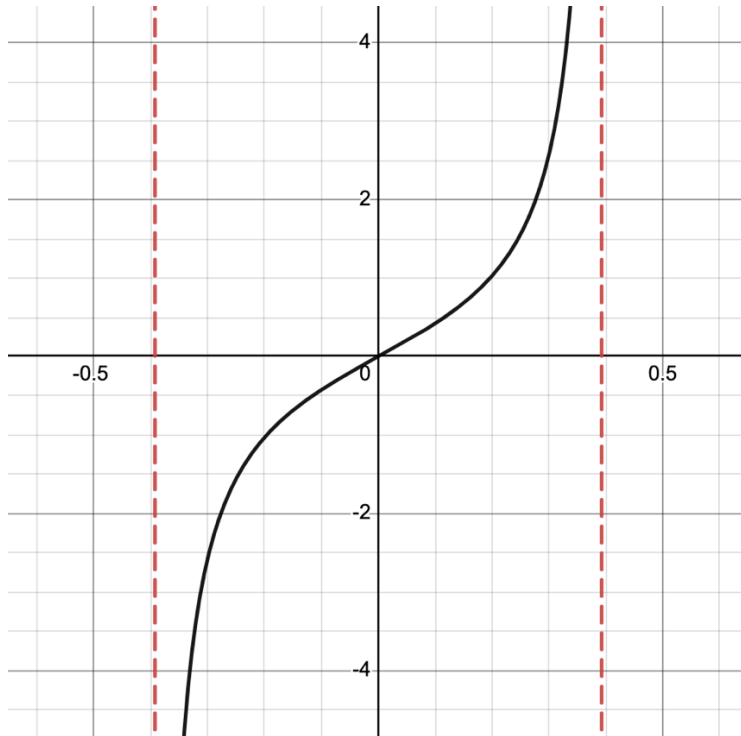
$$12. y = \frac{3}{2}\cot(4\pi x)$$

$$13. y = 3\tan\left(-\frac{x}{4}\right)$$

$$14. y = 2\tan\left(-\frac{x}{6}\right)$$

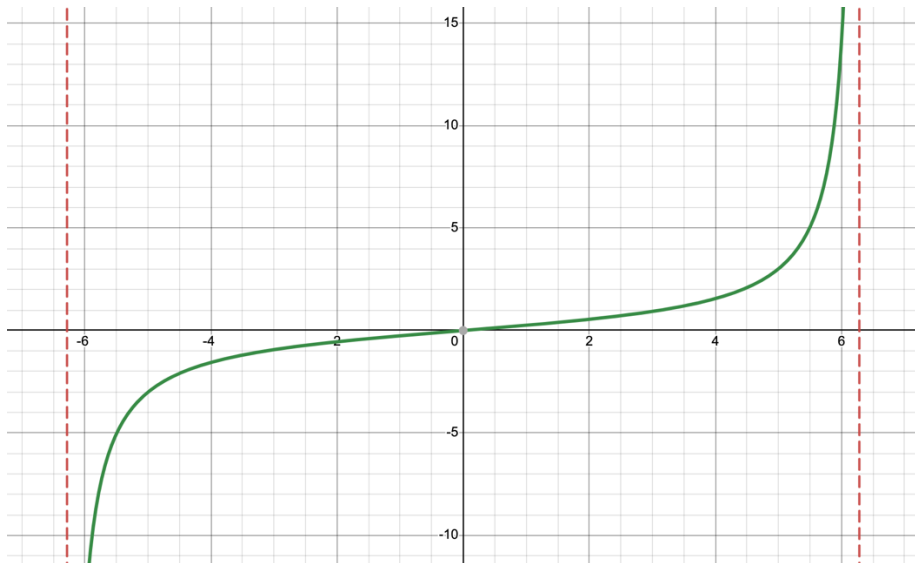
Answers

2.



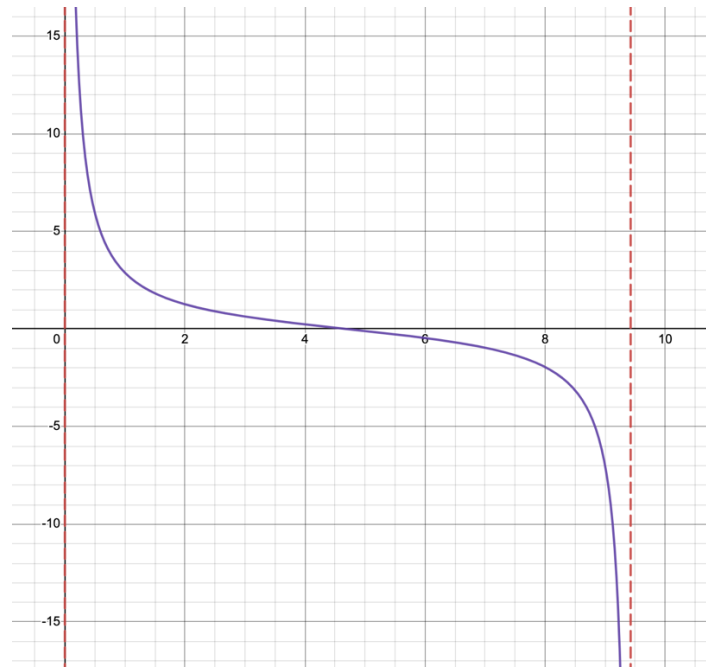
$$\text{Period}=\frac{\pi}{3}, \text{Interval}=\left(0, \frac{\pi}{6}\right), \text{VA: } x = 0, x = \frac{\pi}{6}, \text{x-int: } x = \frac{\pi}{12}$$

4.



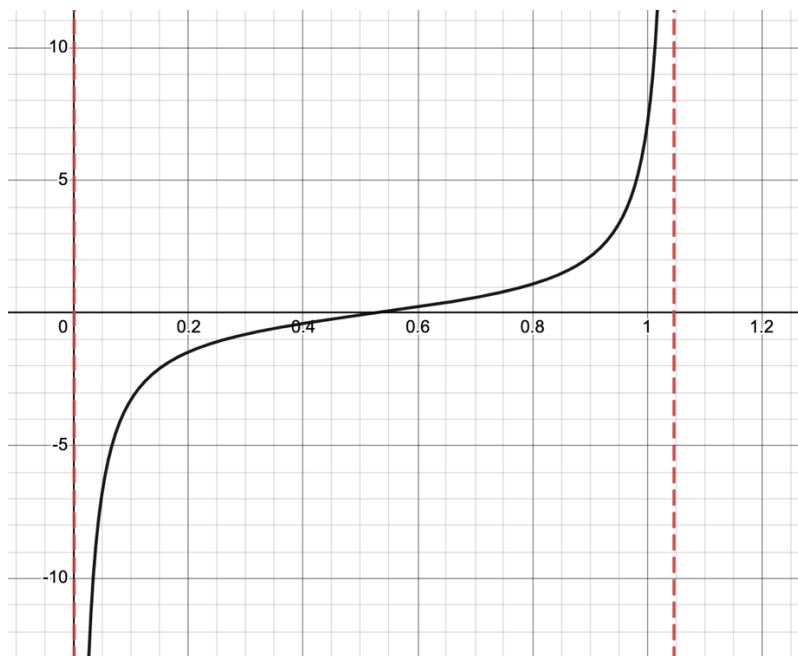
$$\text{Period}=4\pi, \text{Interval}=\left(-2\pi, 2\pi\right), \text{VA: } x = -2\pi, x = 2\pi, \text{x-int: } x = 0$$

6.



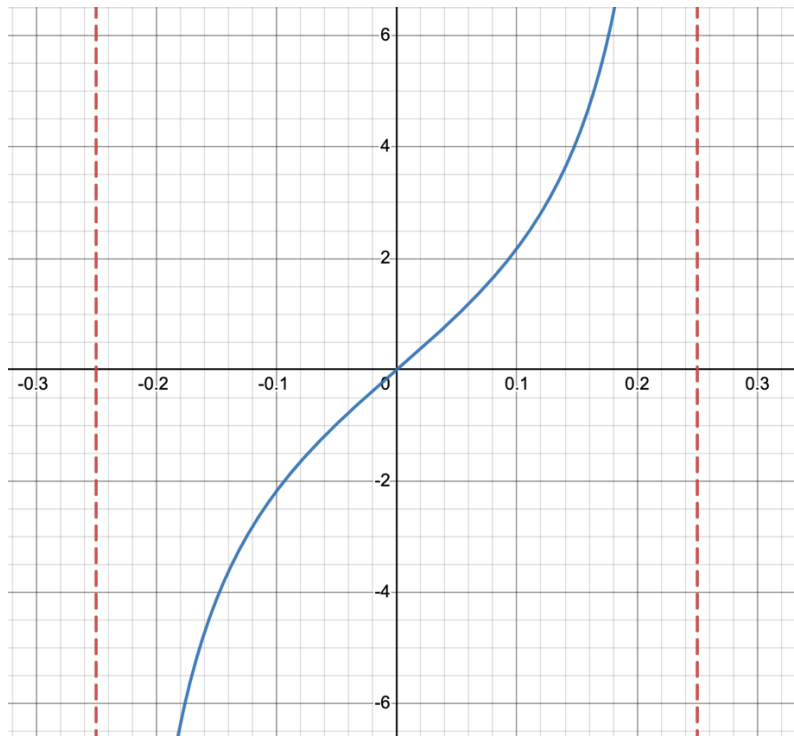
Period= 3π , Interval= $(0, 3\pi)$, VA: $x = 0, x = 3\pi$, x-int: $x = \frac{3\pi}{2}$

8.



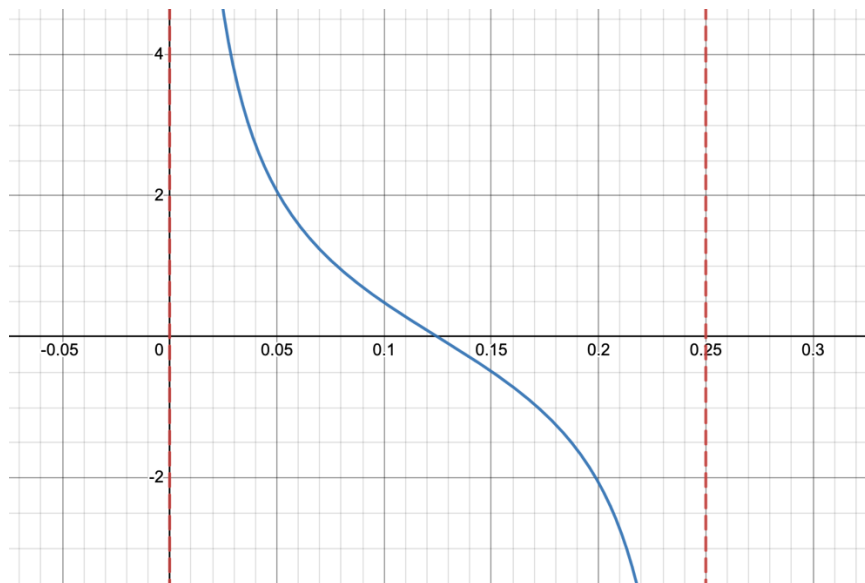
Period= $\frac{\pi}{3}$, Interval= $(0, \frac{\pi}{3})$, VA: $x = 0, x = \frac{\pi}{3}$, x-int: $x = \frac{\pi}{6}$

10.



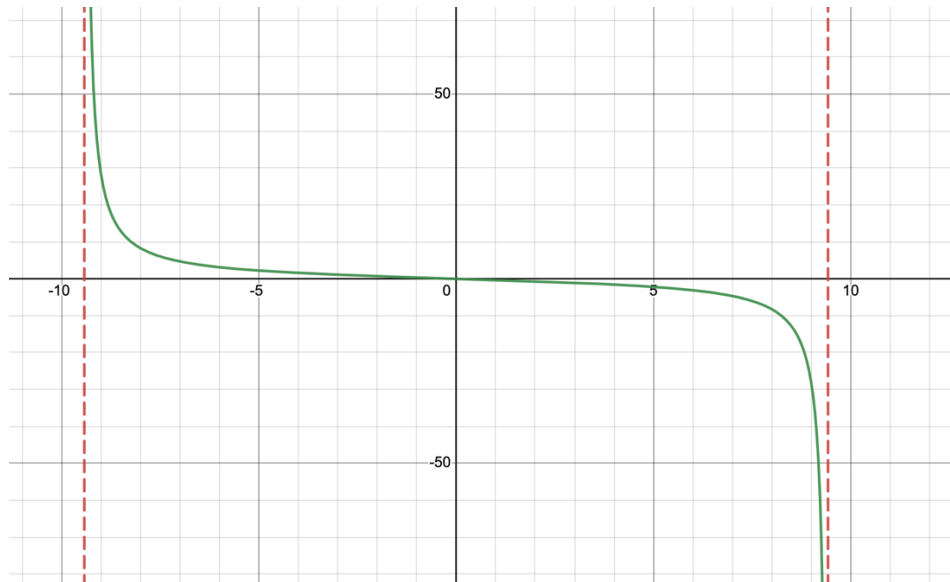
Period = $\frac{1}{2}$, Interval = $(-\frac{1}{4}, \frac{1}{4})$, VA: $x = -\frac{1}{4}, x = \frac{1}{4}$, x-int: $x = 0$

12.



Period = $\frac{1}{4}$, Interval = $(0, \frac{1}{8})$, VA: $x = 0, x = \frac{1}{16}$, x-int: $x = \frac{1}{16}$

14.



Period= 6π , Interval= $(-3\pi, 3\pi)$, VA: $x = -3\pi, x = 3\pi$, x-int: $x = 0$