

Graphing Tangent and Cotangent with Phase Shift

$$y = a \tan[k(x - b)], k > 0$$

$$\text{Period } p = \frac{\pi}{k}$$

Phase Shift b

$$\text{Interval of One Cycle} = \left(b - \frac{\pi}{2k}, b + \frac{\pi}{2k}\right)$$

$$\text{Vertical Asymptotes } x = b - \frac{\pi}{2k} \text{ and } x = b + \frac{\pi}{2k}$$

$$y = a \cot[k(x - b)], k > 0$$

$$\text{Period } p = \frac{\pi}{k}$$

Phase Shift b

$$\text{Interval of One Cycle} = \left(b, b + \frac{\pi}{k}\right)$$

$$\text{Vertical Asymptotes } x = b \text{ and } x = b + \frac{\pi}{k}$$

Determine the period, phase shift, and interval of one cycle, x-int, vertical asymptotes.

1. $y = \tan\left(x - \frac{\pi}{4}\right)$

2. $y = \tan\left(x + \frac{\pi}{4}\right)$

3. $y = \cot\left(x + \frac{\pi}{6}\right)$

4. $y = \cot\left(x - \frac{\pi}{3}\right)$

5. $y = \cot(4x + \pi)$

6. $y = \cot(6x - \pi)$

7. $y = -4 \tan\left[3\left(x - \frac{\pi}{2}\right)\right]$

8. $y = -3 \tan\left[2\left(x + \frac{\pi}{4}\right)\right]$

$$9. y = \frac{1}{2} \cot \left[\frac{1}{3} (x + \pi) \right]$$

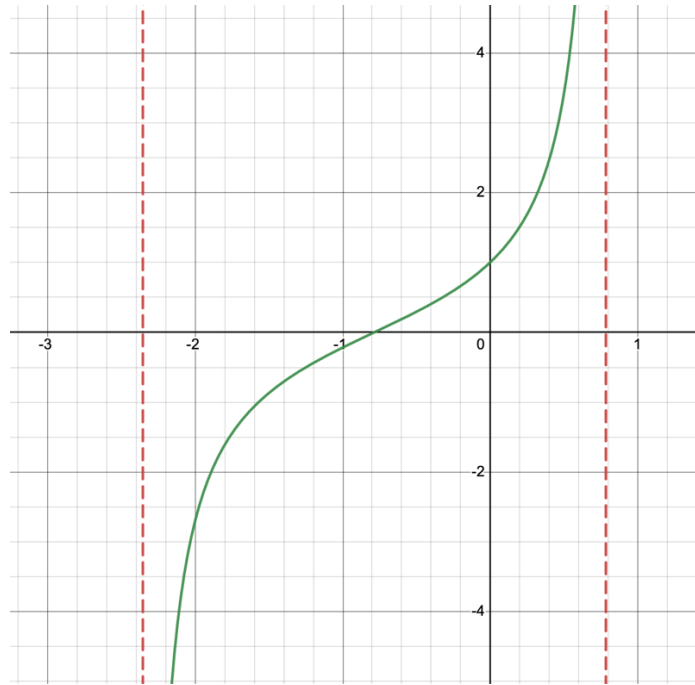
$$10. y = \frac{3}{4} \cot \left[\frac{1}{4} (x - \pi) \right]$$

$$11. y = -\tan \left[\frac{1}{2} \left(x - \frac{\pi}{3} \right) \right]$$

$$12. y = -\tan \left[\frac{1}{2} \left(x + \frac{\pi}{6} \right) \right]$$

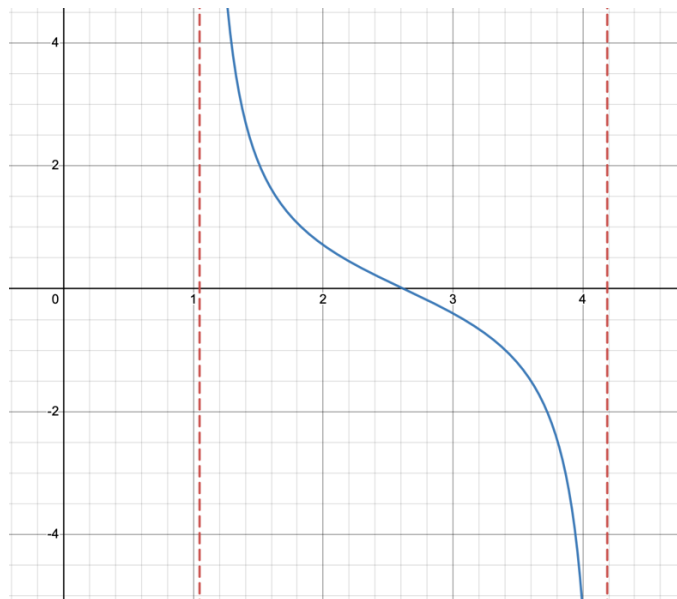
Answers

2.



$$\text{Period} = \pi, \text{Phase} = -\frac{\pi}{4}, \text{Interval} = \left(-\frac{3\pi}{4}, \frac{\pi}{4}\right), \text{VA: } x = -\frac{3\pi}{4}, x = \frac{\pi}{4}, \text{x-int: } x = -\frac{\pi}{4}$$

4.



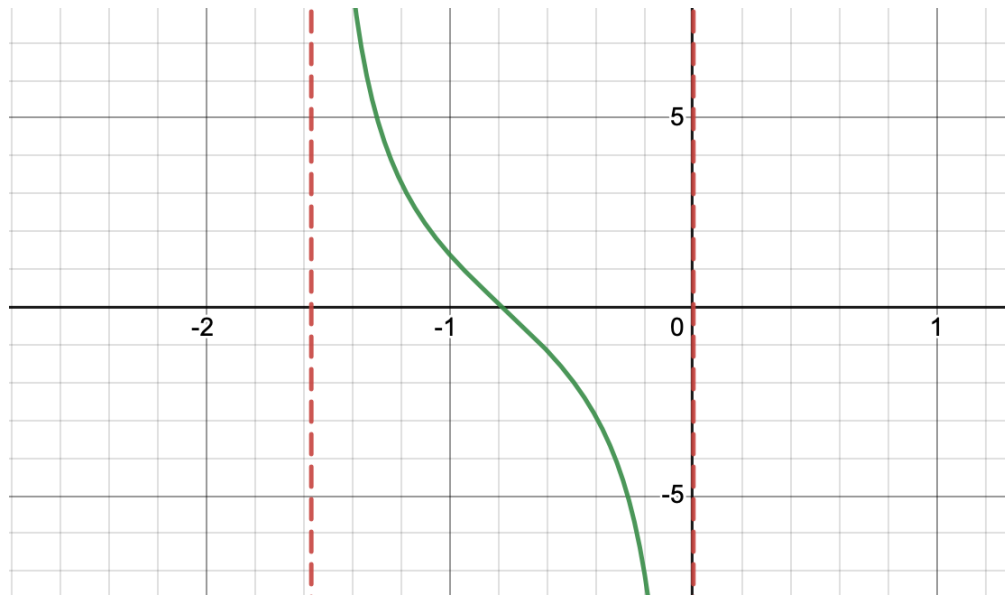
$$\text{Period} = \pi, \text{Phase} = \frac{\pi}{3}, \text{Interval} = \left(\frac{\pi}{3}, \frac{4\pi}{3}\right), \text{VA: } x = \frac{\pi}{3}, x = \frac{4\pi}{3}, \text{x-int: } x = \frac{5\pi}{6}$$

6.



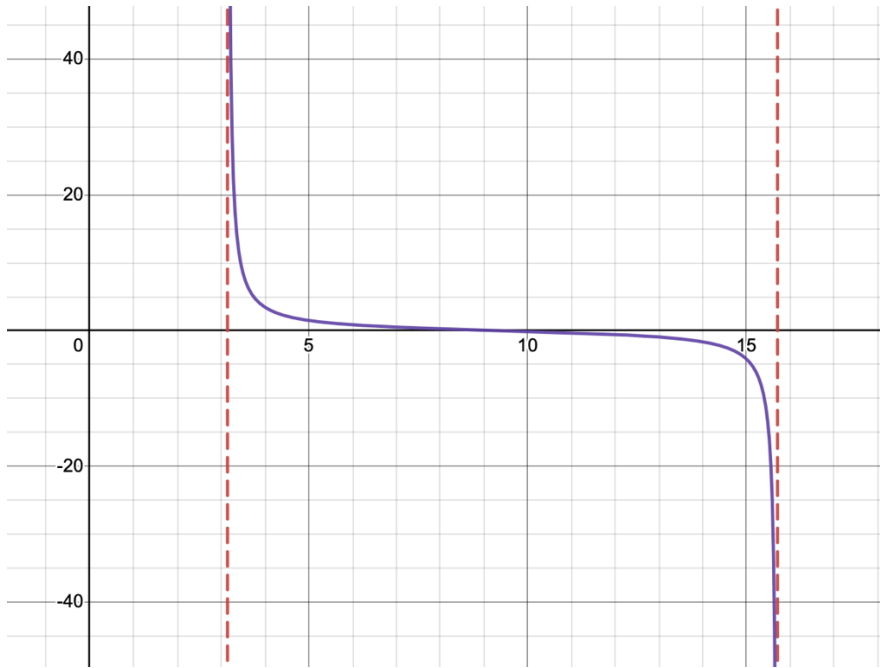
Period = $\frac{\pi}{6}$, Phase = $\frac{\pi}{6}$, Interval = $(\frac{\pi}{6}, \frac{\pi}{3})$, VA: $x = \frac{\pi}{6}, x = \frac{\pi}{3}$, x-int: $x = \frac{\pi}{4}$

8.



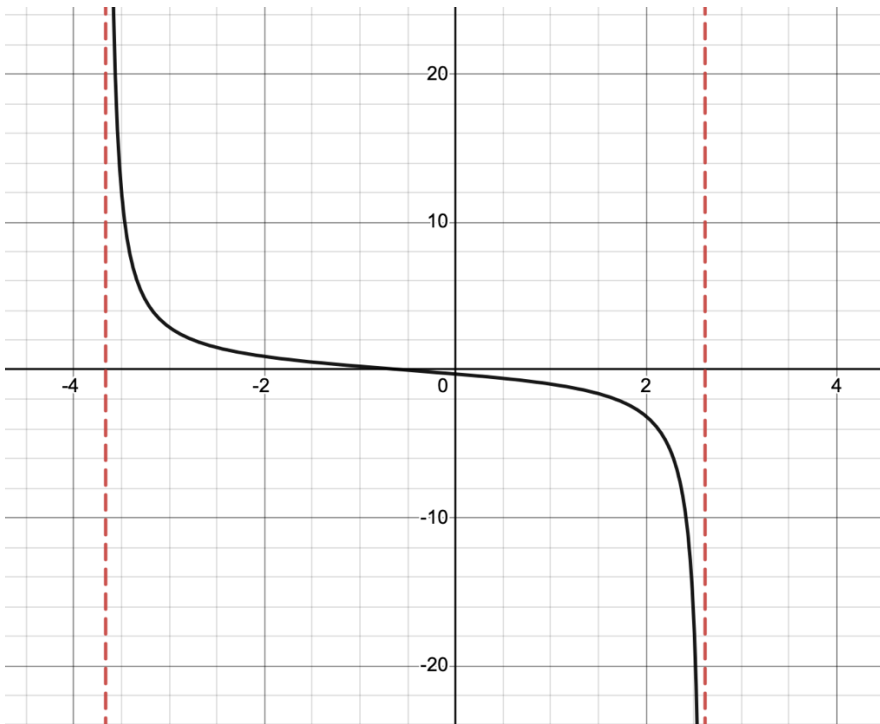
Period = $\frac{\pi}{2}$, Phase = $-\frac{\pi}{4}$, Interval = $(-\frac{\pi}{2}, 0)$, VA: $x = -\frac{\pi}{2}, x = 0$, x-int: $x = -\frac{\pi}{4}$

10.



Period= 4π , Phase= π , Interval= $(\pi, 5\pi)$, VA: $x = \pi, x = 5\pi$, x-int: $x = 3\pi$

12.



Period= 2π , Phase= $-\frac{\pi}{6}$, Interval= $(-\frac{7\pi}{6}, \frac{5\pi}{6})$, VA: $x = -\frac{7\pi}{6}, x = \frac{5\pi}{6}$, x-int: $x = -\frac{\pi}{6}$